Supplementary Material for MIQP-based Layout Design for Building Interiors

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In this document, we provide more details of our method and additional results.

\textbf{Refinement constraint for the horizontal split.} The refinement constraint for the horizontal split is defined as:

\[
\begin{align*}
&x_1 \geq x_1 - \delta \\
&x_1 \leq x_1 \\
&x_1 + w_1 \geq x_1 + w_1 \\
&x_1 + w_1 \leq x_1 + w_1 + \delta \\
y_1 \geq y_1 + d_1 \\
y_1 \leq y_1 + d_1 + \delta \\
x_2 \geq x_2 - \delta \\
x_2 \leq x_2 \\
y_2 \geq y_2 - \delta \\
y_2 \leq y_2 \\
x_2 + w_2 \geq x_2 + w_2 \\
x_2 + w_2 \leq x_2 + w_2 + \delta 
\end{align*}
\]

where \((x_1, y_1, w_1, d_1)\) are parameters of child room \(i_1\), \((x_2, y_2, w_2, d_2)\) are parameters of child room \(i_2\), and \(\delta\) is the refinement range.

\textbf{Additional results.} Fig. 1 shows an interior layout generated according to the listed constraints. All of our constraints are formulated as templates and they can be set easily in our algorithm.

Given the same input (layout domain and constraints), our method can provide multiple layouts that meet all constraints (see Fig. 2). Fig. 3 shows nine layouts of single-storey houses with different boundary complexities. Our method can also generate multi-storey house. Fig. 4 shows eight layouts of two-storey houses. Fig. 5 shows interior layouts generated by our algorithm for different kinds of high-rise residential buildings. We evaluate our method on large-scale examples. Fig. 6 and Fig. 7 show the layout generation processes for the supermarket and office building, respectively. Fig. 8 shows three layouts for office building, supermarket, and shopping mall.

Fig. 9 shows optimization results with different \(\lambda_{\text{cover}}\) (coverage term) and \(\lambda_{\text{size}}\) (size error). We perform a comparison with the stochastic method. We find that our method can generate reasonable results efficiently. Fig. 10 shows layouts generated by two methods, running time for each layout is also shown.

\begin{thebibliography}{1}
\bibitem{MSK10} \textsc{Merrill P., Schufza E., Koltun V.:} Computer-generated residential building layouts. In \textit{ACM Transactions on Graphics (TOG)} (2010), vol. 29, ACM, p. 181. 8
\end{thebibliography}
Figure 1: An interior layout is generated according to the constraints listed in the table. In the size constraint, $w(\cdot)$ and $d(\cdot)$ denote the width and depth operators, respectively. $r(\cdot)$ is the aspect ratio operator. If a room is adjacent to the boundary, $Y$ is assigned in the boundary constraint column, otherwise $N$ is set for the room. Please note that the inside constraint and non-overlap constraint are not listed here.

<table>
<thead>
<tr>
<th>Room</th>
<th>Size target</th>
<th>Size constraint</th>
<th>Aspect ratio constraint</th>
<th>Boundary constraint</th>
<th>Adjacency constraint</th>
<th>Adjacency constraint for three rooms</th>
</tr>
</thead>
<tbody>
<tr>
<td>Foyer</td>
<td>$w($Foyer$) = 2.03$, $d($Foyer$) = 2.92$</td>
<td>$1.02 \geq w($Foyer$) \geq 3.05$, $1.46 \geq d($Foyer$) \geq 4.38$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Corridor</td>
<td>$w($Corridor$) \leq 1.80$, $d($Corridor$) \geq 2.55$</td>
<td>$1.76 \geq w($Corridor$) \geq 5.27$, $0.93 \geq d($Corridor$) \geq 1.76$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Utility</td>
<td>$w($Utility$) = 0.19$, $d($Utility$) = 2.70$</td>
<td>$0.19 \geq w($Utility$) \geq 2.34$, $0.95 \geq d($Utility$) \geq 1.76$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Toilet</td>
<td>$w($Toilet$) \leq 1.55$, $d($Toilet$) \geq 2.55$</td>
<td>$0.94 \geq w($Toilet$) \geq 2.82$, $1.18 \geq d($Toilet$) \geq 3.53$</td>
<td></td>
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</tr>
<tr>
<td>Kitchen</td>
<td>$w($Kitchen$) \leq 5.20$, $d($Kitchen$) \geq 2.26$</td>
<td>$1.64 \geq w($Kitchen$) \geq 4.92$, $1.13 \geq d($Kitchen$) \geq 3.19$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Living room</td>
<td>$w($Living room$) \leq 5.20$, $d($Living room$) \geq 4.38$</td>
<td>$1.70 \geq w($Living room$) \geq 5.09$, $2.17 \geq d($Living room$) \geq 6.51$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Master bedroom</td>
<td>$w($Master bedroom$) \leq 1.80$, $d($Master bedroom$) \geq 2.21$</td>
<td>$1.60 \geq w($Master bedroom$) \geq 4.80$, $2.21 \geq d($Master bedroom$) \geq 6.63$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Bedroom</td>
<td>$w($Bedroom$) \leq 2.45$, $d($Bedroom$) \geq 3.96$</td>
<td>$1.43 \geq w($Bedroom$) \geq 4.20$, $1.98 \geq d($Bedroom$) \geq 5.94$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Bathroom</td>
<td>$w($Bathroom$) \leq 1.80$, $d($Bathroom$) \geq 2.55$</td>
<td>$0.94 \geq w($Bathroom$) \geq 2.62$, $1.18 \geq d($Bathroom$) \geq 3.53$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Figure 2: Given the same input (i.e., layout domain and constraints), our method generates three different layouts. The position of the front door is given.
Figure 3: Nine layouts of single-storey house synthesized using our algorithm. The complexity of the house boundary gradually increases.
Figure 4: Seven layouts of two-storey house generated using our method. The stairs are consistent between two floors. For (1,2,3), the layout of the first floor is shown on the bottom, the layout of the second floor is shown on the top. For (4,5,6,7), the layout of the first floor is shown on the left, the layout of the second floor is shown on the right.
Figure 5: Layouts of residential building generated using our method. (a,b) two symmetric apartments on one floor; (c,d) two asymmetric apartments on one floor; (e,f) four apartments on one floor.
Figure 6: An interior layout of the supermarket is generated by our hierarchical framework.

Figure 7: An interior layout of the office building is generated by our hierarchical framework.
Figure 8: Three large-scale layouts generated by our hierarchical algorithm. (a) office building, (b) supermarket, (c) shopping mall. The boundaries are abstracted from real cases which are shown in the top-right of each layout. (d) shows the number of rooms, the number of constraints, and the running time for each layout.

Figure 9: Layouts generated by our algorithm using different weights: $\lambda_{\text{cover}}$ and $\lambda_{\text{size}}$. A small $\lambda_{\text{cover}}$ gives rise to complex room shapes, while a small $\lambda_{\text{size}}$ leads to layouts with large size error.
Figure 10: Comparison with the stochastic approach [MSK10]. We show comparisons on rows. Left column: layouts generated by our algorithm. Right column: layouts generated by the stochastic method. Running time of each layout is shown below. Uncovered regions are highlighted in red.